

# Cryptographic Protocols

## Exercise 13

### 13.1 Adversaries in the Player Elimination Framework

Consider any non-robust but detectable protocol run in the Player Elimination Framework with  $t$  corrupted parties. Find a strategy for the adversary that maximizes the communicated bits among honest parties.

### 13.2 Berlekamp-Welch-Decoding

Consider the local reconstruction protocol from the lecture where party  $P_i$  receives shares  $s_i$  of a degree- $d$ -sharing (a polynomial  $g$  with  $\deg(g) \leq d$ ) of some secret  $s$ . Let  $A \subseteq \{1, \dots, n\}$  (where  $|A| \leq t < \frac{n}{3}$ ) be the indices of corrupted parties  $P_j$ , which sent values with  $s_j \neq g(\alpha_j)$ .

Consider the polynomials  $e(x) = \prod_{i \in A} (x - \alpha_i)$  and  $p(x) = g(x) \cdot e(x)$ .

a) Show that for all  $j \in \{1, \dots, n\}$  we have  $p(\alpha_j) = s_j \cdot e(\alpha_j)$ .

b) Show that for  $d < n - 2t$  party  $P_i$  can efficiently recover  $g(x)$ .

### 13.3 Sharings of Zero

a) Describe a passively secure protocol that allows  $n$  players to jointly generate  $\Omega(n)$  random sharings of 0 and prove its security.

b) Modify your protocol such that it becomes actively-secure with abort, and prove its security.