

Cryptographic Protocols

Exercise 11

11.1 Information-Theoretic Commitment Transfer Protocol

- a) Consider the information-theoretically secure (distributed) commitment scheme from the lecture. Describe the state achieved by the COMMIT protocol, i.e., describe the output of each player and the consistency condition among these outputs.
- b) Design a commitment transfer protocol CTP for a commitment created via COMMIT. Show that your protocol is secure. How many corrupted players can be tolerated?

11.2 Information-Theoretic Commitment Multiplication Protocol

- a) Show that the commitment multiplication protocol (CMP) from the lecture is secure for $t < n/3$, i.e., that it satisfies the properties:
 1. CORRECTNESS: At the end of CMP, either the dealer D is committed to c such that $c = ab$, or it is publicly seen that D is corrupted.
 2. PRIVACY: Up to t players (not including D) obtain no information on the values a and b .
- b) Show that the protocol CMP is insecure if $t \geq n/3$.
HINT: Show that if $n = 3t$, then an adversary corrupting t players (including D) can achieve that at the end of the protocol player D is committed to some $c' \neq ab$.

11.3 Information-Theoretic Commit Protocol

The Commit-Protocol from the lecture requires up to t rounds of accusations (Step 3). In this exercise, we prove that two rounds of accusations are sufficient.

Prove that after two rounds of accusations, either

- the dealer is disqualified ($> t$ accusations in rounds 1–2), OR
- all accusations in Round 2 are by corrupted parties.

Use the following notation: Let H denote the set of honest parties and A_i denote the set of parties accusing the dealer in Round i (for $i \in \{1, 2\}$).

Hint: If $|A_1| \leq t$, then $H \setminus A_1$ define a unique degree- t polynomial $f'(x, y)$.